repAIrC: A Tool for Ensuring Data Consistency
by *Means of Active Integrity Constraints*

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Abstract: Consistency of knowledge repositories is of prime importance in organization management. Integrity constraints are a well-known vehicle for specifying data consistency requirements in knowledge bases; in particular, active integrity constraints go one step further, allowing the specification of preferred ways to overcome inconsistent situations in the context of database management.

This paper describes a tool to validate an SQL database with respect to a given set of active integrity constraints, proposing possible repairs in case the database is inconsistent. The tool is able to work with the different kinds of repairs proposed in the literature, namely simple, founded, well-founded and justified repairs. It also implements strategies for parallelizing the search for them, allowing the user both to compute partitions of independent or stratified active integrity constraints, and to apply these partitions to find repairs of inconsistent databases efficiently in parallel.

1 INTRODUCTION

There is a generalized consensus that knowledge repositories are a key ingredient in the whole process of Knowledge Management, cf. (Duhon, 1998; König, 2012). Furthermore, being able to rely upon the consistency of the information they provide is paramount to any business whatsoever. Databases and database management systems, by far the most common framework for knowledge storage and retrieval, have been around for many years now, and have evolved substantially, at pace with information technology. In this paper, we are focusing on the important aspect of database consistency.

Typical database management systems allow the user to specify integrity constraints on the data as logical statements that are required to be satisfied at any given point in time. The classical problem is how to guarantee that such constraints still hold after updating databases (Abiteboul, 1988), and what repairs have to be made when the constraints are violated (Katsuno and Mendelzon, 1991), without making any assumptions about how the inconsistencies came about. Repairing an inconsistent database (Eiter and Gottlob, 1992) is a highly complex process; also,

it is widely accepted that human intervention is often necessary to choose an adequate repair. That said, every progress towards automation in this field is nevertheless important.

In particular, the framework of active integrity constraints (Flesca et al., 2004; Caroprese and Truszczyński, 2011) was introduced more recently with the goal of giving operational mechanisms to compute repairs of inconsistent databases. This framework has subsequently been extended to consider preferences (Caroprese et al., 2007) and to find "best" repairs automatically (Cruz-Filipe et al., 2013) and efficiently (Cruz-Filipe, 2014).

Active integrity constraints (AICs) seem to be a promising framework for the purpose of achieving reliability in information retrieval:

- AICs are expressive enough to encompass the majority of integrity constraints that are typically found in practice;

- AICs allow the definition of preferred ways to calculate repairs, through specific actions to be taken in specific inconsistent situations;

- AICs provide mechanisms to resolve inconsistencies while the database is in use;

- AICs can enhance databases to provide a basis for self-healing autonomic systems.

To the best of our knowledge, no real-world implementation of an AIC–enhanced database system exists today. This paper presents a prototype tool that implements the tree–based algorithms for computing repairs presented in (Caroprese and Truszczyński, 2011; Cruz-Filipe et al., 2013). While not yet ready for productive deployment, this implementation can work successfully with database management systems working in the SQL framework, and is readily extendible to other (nearly arbitrary) database management systems thanks to its modular design.

This paper is structured as follows. Section 2 recapitulates previous work on active integrity constraints and repair trees. Section 3 introduces our tool, `repAIrC`, and describes its implementation, focusing on the new theoretical results that were necessary to bridge the gap between theory and practice. Section 4 then discusses how parallel computation capabilities are incorporated in `repAIrC` to make the search for repairs more efficient. Section 5 summarizes our achievements and gives a brief outlook into future developments.

2 ACTIVE INTEGRITY CONSTRAINTS

Active integrity constraints (AICs) were introduced in (Flesca et al., 2004) and further explored in (Caroprese et al., 2009; Caroprese and Truszczyński, 2011), which define the basic concepts and prove complexity bounds for the problem of repairing inconsistent databases. These authors introduce declarative semantics for different types of repairs, obtaining their complexity results by means of a translation into revision programming. In practice, however, this does not yield algorithms that are applicable to real-life databases; for this reason, a direct operational semantics for AICs was proposed in (Cruz-Filipe et al., 2013), presenting database-oriented algorithms for finding repairs. The present paper describes a tool that can actually execute these algorithms in collaboration with an SQL database management system.

2.1 Syntax and Declarative Semantics

For the purpose of this work, we can view a database simply as a set of atomic formulas over a typed function-free first-order signature Σ, which we will assume throughout to be fixed. Let $\mathcal{A}t$ be the set of closed atomic formulas over Σ. A database I *entails*

literal L, $I \models L$, if $L \in \mathcal{A}t$ and $L \in I$, or if L is not a with $a \in \mathcal{A}t$ and $a \notin I$.

An integrity constraint is a clause

$$L_1, \ldots, L_m \supset \bot$$

where each L_i is a literal over Σ, with intended semantics that $\forall(L_1 \wedge \ldots \wedge L_m)$ should not hold. As is usual in logic programming, we require that if L_i contains a negated variable x, then x already occurs in $L_1, \ldots, L_{i-1}$. We say that I *satisfies* integrity constraint r, $I \models r$, if, for every instantiation θ of the variables in r, it is the case that $I \not\models L\theta$ for some L in r; and I satisfies a set η of integrity constraints, $I \models \eta$, if it satisfies each integrity constraint in η.

If $I \not\models \eta$, then I may be updated through *update actions* of the form $+a$ and $-a$, where $a \in \mathcal{A}t$, stating that a is to be inserted in or deleted from I, respectively. A set of update actions $\mathcal{U}$ is *consistent* if it does not contain both $+a$ and $-a$, for any $a \in \mathcal{A}t$; in this case, I can be updated by $\mathcal{U}$, yielding the database

$$I \circ \mathcal{U} = (I \cup \{a \mid +a \in \mathcal{U}\}) \setminus \{a \mid -a \in \mathcal{U}\}.$$

The problem of database repair is to find $\mathcal{U}$ such that $I \circ \mathcal{U} \models \eta$.

Definition 1. *Let I be a database and η a set of integrity constraints. A* weak repair *for $\langle I, \eta \rangle$ is a consistent set $\mathcal{U}$ of update actions such that: (i) every action in $\mathcal{U}$ changes I; and (ii) $I \circ \mathcal{U} \models \eta$. A* repair *for $\langle I, \eta \rangle$ is a weak repair $\mathcal{U}$ for $\langle I, \eta \rangle$ that is minimal w.r.t. set inclusion.*

The distinction between weak repairs and repairs embodies the standard principle of *minimality of change* (Winslett, 1990).

The problem of deciding whether there exists a (weak) repair for an inconsistent database is *NP*-complete (Caroprese and Truszczyński, 2011). Furthermore, simply detecting that a database is inconsistent does not give any information on how it can be repaired. In order to address this issue, those authors proposed active integrity constraints (AICs), which guide the process of selection of a repair by pairing literals with the corresponding update actions.

In the syntax of AICs, we extend the notion of update action by allowing variables. Given an action α, the literal corresponding to it is $\mathsf{lit}(\alpha)$, defined as a if $\alpha = +a$ and not a if $\alpha = -a$; conversely, the update action corresponding to a literal L, $\mathsf{ua}(L)$, is $+a$ if $L = a$ and $-a$ if $L = $ not a. The *dual* of a is not a, and conversely; the dual of L is denoted L^D. An *active integrity constraint* is thus an expression r of the form

$$L_1, \ldots, L_m \supset \alpha_1 \mid \ldots \mid \alpha_k$$

where the L_i (in the *body* of r, $\mathsf{body}\,(r)$) are literals and the α_j (in the *head* of r, $\mathsf{head}\,(r)$) are update actions, such that

$$\left\{\mathsf{lit}(\alpha_1)^D,\ldots,\mathsf{lit}(\alpha_k)^D\right\} \subseteq \{L_1,\ldots,L_m\}\,.$$

The set $\mathsf{lit}(\mathsf{head}\,(r))^D$ contains the *updatable* literals of r. The *non-updatable* literals of r form the set $\mathsf{nup}(r) = \mathsf{body}\,(r) \setminus \mathsf{lit}\,(\mathsf{head}\,(r))^D$.

The natural semantics for AICs restricts the notion of weak repair.

Definition 2. *Let I be a database, η a set of AICs and $\mathcal{U}$ be a (weak) repair for $\langle I,\eta \rangle$. Then $\mathcal{U}$ is a founded (weak) repair for $\langle I,\eta \rangle$ if, for every action $\alpha \in \mathcal{U}$, there is a closed instance r' of $r \in \eta$ such that $\alpha \in \mathsf{head}\,(r')$ and $I \circ \mathcal{U} \models L$ for every $L \in \mathsf{body}\,(r') \setminus \left\{\mathsf{lit}(\alpha)^D\right\}$.*

The problem of deciding whether there exists a weak founded repair for an inconsistent database is again *NP*-complete, while the similar problem for founded repairs is Σ_2^P-complete. Despite their natural definition, founded repairs can include circular support for actions, which can be undesirable; this led to the introduction of justified repairs (Caroprese and Truszczyński, 2011).

We say that a set $\mathcal{U}$ of update actions is *closed* under r if $\mathsf{nup}(r) \subseteq \mathsf{lit}(\mathcal{U})$ implies $\mathsf{head}\,(r) \cap \mathcal{U} \neq \emptyset$, and it is closed under a set η of AICs if it is closed under every closed instance of every rule in η. In particular, every founded weak repair for $\langle I,\eta \rangle$ is by definition closed under η.

A closed update action $+a$ (resp. $-a$) is a *no-effect* action w.r.t. $(I, I \circ \mathcal{U})$ if $a \in I \cap (I \circ \mathcal{U})$ (resp. $a \notin I \cup (I \circ \mathcal{U})$). The set of all no-effect actions w.r.t. $(I, I \circ \mathcal{U})$ is denoted by $\mathsf{ne}\,(I, I \circ \mathcal{U})$. A set of update actions $\mathcal{U}$ is a justified action set if it coincides with the set of update actions forced by the set of AICs and the database before and after applying $\mathcal{U}$ (Caroprese and Truszczyński, 2011).

Definition 3. *Let I be a database and η a set of AICs. A consistent set $\mathcal{U}$ of update actions is a justified action set for $\langle I,\eta \rangle$ if it is a minimal set of update actions containing $\mathsf{ne}\,(I, I \circ \mathcal{U})$ and closed under η. If $\mathcal{U}$ is a justified action set for $\langle I,\eta \rangle$, then $\mathcal{U} \setminus \mathsf{ne}\,(I, I \circ \mathcal{U})$ is a justified weak repair for $\langle I,\eta \rangle$.*

In particular, it has been shown that justified repairs are always founded (Caroprese and Truszczyński, 2011). The problem of deciding whether there exist justified weak repairs or justified repairs for $\langle I,\eta \rangle$ is again Σ_2^P-complete problem, becoming *NP*-complete if one restricts the AICs to contain only one action in their head (*normal* AICs).

2.2 Operational Semantics

The declarative semantics of AICs is not very satisfactory, as it does not capture the operational nature of rules. In particular, the quantification over all no-effect actions in the definition of justified action set poses a practical problem. Therefore, an operational semantics for AICs was proposed in (Cruz-Filipe et al., 2013), which we now summarize.

Definition 4. *Let I be a database and η be a set of AICs.*

- *The* repair tree *for $\langle I,\eta \rangle$, $T_{\langle I,\eta \rangle}$, is a labeled tree where: nodes are sets of update actions; each edge is labeled with a closed instance of a rule in η; the root is $\emptyset$; and for each consistent node n and closed instance r of a rule in η, if $I \circ n \not\models r$ then for each $L \in \mathsf{body}\,(r)$ the set $n' = n \cup \left\{\mathsf{ua}(L)^D\right\}$ is a child of n, with the edge from n to n' labeled by r.*

- *The* founded repair tree *for $\langle I,\eta \rangle$, $T_{\langle I,\eta \rangle}^f$, is constructed as $T_{\langle I,\eta \rangle}$ but requiring that $\mathsf{ua}(L)$ occur in the head of some closed instance of a rule in η.*

- *The* well-founded repair tree *for $\langle I,\eta \rangle$, $T_{\langle I,\eta \rangle}^{wf}$, is also constructed as $T_{\langle I,\eta \rangle}$ but requiring that $\mathsf{ua}(L)$ occur in the head of the rule being applied.*

- *The* justified repair tree *for $\langle I,\eta \rangle$, $T_{\langle I,\eta \rangle}^j$, has nodes that are* pairs *of sets of update actions $\langle \mathcal{U}, \mathcal{J} \rangle$, with root $\langle \emptyset, \emptyset \rangle$. For each node n and closed instance r of a rule in η, if $I \circ \mathcal{U}_n \not\models r$, then for each $\alpha \in \mathsf{head}\,(r)$ there is a descendant n' of n, with the edge from n to n' labeled by r, where: $\mathcal{U}_{n'} = \mathcal{U}_n \cup \{\alpha\}$; and $\mathcal{J}_{n'} = (\mathcal{J}_n \cup \{\mathsf{ua}(\mathsf{nup}(r))\}) \setminus \mathcal{U}_n$.*

The properties of repair trees are summarized in the following results, proved in (Cruz-Filipe et al., 2013).

Theorem 1. *Let I be a database and η be a set of AICs. Then:*

1. *$T_{\langle I,\eta \rangle}$ is finite.*
2. *Every consistent leaf of $T_{\langle I,\eta \rangle}$ is labeled by a weak repair for $\langle I,\eta \rangle$.*
3. *If $\mathcal{U}$ is a repair for $\langle I,\eta \rangle$, then there is a branch of $T_{\langle I,\eta \rangle}$ ending with a leaf labeled by $\mathcal{U}$.*
4. *If $\mathcal{U}$ is a founded repair for $\langle I,\eta \rangle$, then there is a branch of $T_{\langle I,\eta \rangle}^f$ ending with a leaf labeled by $\mathcal{U}$.*
5. *If $\mathcal{U}$ is a justified repair for $\langle I,\eta \rangle$, then there is a branch of $T_{\langle I,\eta \rangle}^j$ ending with a leaf labeled by $\mathcal{U}$.*
6. *If η is a set of normal AICs and $\langle \mathcal{U}, \mathcal{J} \rangle$ is a leaf of $T_{\langle I,\eta \rangle}^j$ with $\mathcal{U}$ consistent and $\mathcal{U} \cap \mathcal{J} = \emptyset$, then $\mathcal{U}$ is a justified repair for $\langle I,\eta \rangle$.*

Not all leaves will correspond to repairs of the desired kind; in particular, there may be weak repairs in repair trees. Also, both $T^f_{\langle I,\eta \rangle}$ and $T^j_{\langle I,\eta \rangle}$ typically contain leaves that do not correspond to founded or justified (weak) repairs – otherwise the problem of deciding whether there exists a founded or justified weak repair for $\langle I,\eta \rangle$ would be solvable in non-deterministic polynomial time. The leaves of the well-founded repair tree for $\langle I,\eta \rangle$ correspond to a new type of weak repairs, called *well-founded weak repairs*, not considered in the original works on AICs.

2.3 Parallel Computation of Repairs

The computation of founded or justified repairs can be improved by dividing the set of AICs into independent sets that can be processed independently, simply merging the computed repairs at the end (Cruz-Filipe, 2014). Here, we adapt the definitions given therein to the first-order scenario. Two sets of AICs η_1 and η_2 are independent if the same atom does not occur in a literal in the body of a closed instance of two distinct rules $r_1 \in \eta_1$ and $r_2 \in \eta_2$. If η_1 and η_2 are independent, then repairs for $\langle I,\eta_1 \cup \eta_2 \rangle$ are exactly the unions of a repair for $\langle I,\eta_1 \rangle$ and $\langle I,\eta_2 \rangle$; furthermore, the result still holds if one considers founded, well-founded or justified repairs.

If an atom occurs in a literal in the body of a closed instance of a rule in η_2 and in an action in the head of a closed instance of a rule in η_1, but not conversely, then we say that η_1 *precedes* η_2. Founded/justified (but not well-founded) repairs for $\eta_1 \cup \eta_2$ can be computed in a stratified way, by first repairing I w.r.t. η_1, and then repairing the result w.r.t. η_2.

Splitting a set of AICs into independent sets or stratifying it can be solved using standard algorithms on graphs, as we describe in Section 4.

3 THE TOOL

The tool `repAIrC` is implemented in Java, and its simplified UML class diagram can be seen in Figure 1. Structurally, this tool can be split into four main separate components, centered on the four classes marked in bold in that figure.

- Objects of type `AIC` implement active integrity constraints.
- Implementations of interface `DB` provide the necessary tools to interact with a particular database management system; currently, we provide functionality for SQL databases supported by JDBC.

- Objects of type `RepairTree` correspond to concrete repair trees; their exact type will be the subclass corresponding to a particular kind of repairs.
- Class `RunRepairGUI` provides the graphical interface to interact with the user.

An important design aspect has to do with extensibility and modularity. A first prototype focused on the construction of repair trees, and used simple text files to mimick databases as lists of propositional atoms, in the style of (Caroprese and Truszczyński, 2011; Cruz-Filipe et al., 2013). Later, parallelization capabilities were added (as explained in Section 4), requiring changes only to `RepairController` – the class that controls the execution of the whole process. Likewise, the extension of `repAIrC` to SQL databases and the addition of the stratification mechanism only required localized changes in the classes directly concerned with those processes.

The next subsections detail the implementation of the classes `AIC`, `DB`, `RepairTree` and `RunRepairTreeGUI`.

3.1 Representing Active Integrity Constraints

In the practical setting, it makes sense to diverge a little from the theoretical definition of AICs.

- Real-world tables found in DBs contain many columns, most of which are typically irrelevant for a given integrity constraint.
- The columns of a table are not static, i.e., columns are usually added or removed during a database's lifecycle.
- The order of columns in a table should not matter, as they are identified by a unique column name.

To deal pragmatically with these three aspects, we will write atoms using a more database-oriented notation, allowing the arguments to be provided in any order, but requiring that the column names be provided. The special token `$` is used as first character of a variable. So, for example, the literal
`hasInsurance(firstName=$X, type='basic')`
will match any entry in table `hasInsurance` having value `basic` in column `type` and any value in column `firstName`; this table may additionally have other columns. Negative literals are preceded by the keyword `NOT`, while actions must begin with + or -. Literals and actions are separated by commas, and the body and head of an AIC are separated by `->`. The AIC is finished when `;` is encountered, thus allowing constraints to span several lines.

AICs are provided in a text file, which is parsed by a parser generated automatically using JavaCC
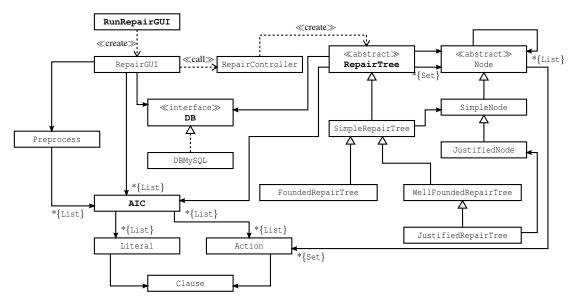
Figure 1: Class diagram for repAIrC.

and transformed into objects of type `AIC`. These contain a body and a head, which are respectively `List<Literal>` and `List<Action>`; for consistency with the underlying theory, `Literal` and `Action` are implemented separately, although their objects are isomorphic: they contain an object of type `Clause` (which consists of the name of a table in the database and a list of pairs column name/value) and a flag indicating whether they are positive/negated (literals) or additions/removals (actions).

Example 1. *Consider the following active integrity constraints for an employee database. The first states that the boss (as specified in the* category *table) cannot be a junior employee (i.e., have an entry in the* junior *table); the second states that every junior employee must have some basic insurance (as specified in the* insured *table).*

$$\mathsf{junior}(X), \mathsf{category}(\mathsf{boss}, X) \supset -\mathsf{junior}(X)$$

$$\mathsf{junior}(X), \mathsf{not\ insured}(X, \mathsf{basic})$$
$$\supset +\mathsf{insured}(X, \mathsf{basic})$$

These are written in the concrete text-based syntax of the repAIrC *tool as*

```
junior(id = $X),
  category(type = boss, empId = $X)
  -> - junior(id = $X);

junior(id = $X),
  NOT insured(empId = $X, type = basic)
  -> + insured(empId = $X, type = basic);
```

respectively, assuming the corresponding column names for the atributes. Note that, thanks to our usage of explicit column naming, the column names for the same variable need not have identical designations.

3.2 Interfacing with the Database

Database operations (queries and updates) are defined in the `DB` interface, which contains the following methods.

- `getUpdateActions(AIC aic)`: queries the database for all the instances of `aic` that are not satisfied in its current state, returning a `Collection<Collection<Action>>` that contains the corresponding instantiations of the head of `aic`.

- `update(Collection<Action> actions)`: applies all update actions in `actions` to the database (void).

- `undo(Collection<Action> actions)`: undoes the effect of all update actions in `actions` (void).

- `aicsCompatible(Collection<AIC> aics)`: checks that all the elements of `aics` are compatible with the structure of the database.

- `disconnect()`: disconnects from the database (void). The connection is established when the object is originally constructed.

Some of these methods require more detailed comments. The construction of the repair tree also requires that the database be changed interactively, but upon conclusion the database should be returned to its original state. In theory, this would be achievable by applying the `update` method with the duals of the actions that were used to change the database; but this turns out not to be the case for deletion actions. Since the AICs may underspecify the entries in the database

(because some fields are left implicit), the implementation of `update` must take care to store the values of all rows that are deleted from the database. In turn, the `undo` method will read this information every time it has to undo a deletion action, in order to find out exactly what entries to re-add.

The method `aicsCompatible` is necessary because the AICs are given independently of the database, but they must be compatible with its structure – otherwise, all queries will return errors. Including this method in the interface allows the AICs to be tested before any queries are made, thus significantly reducing the number of exceptions that can occur during program execution.

Currently, `repAIrC` includes an implementation `DBMySQL` of `DB`, which works with SQL databases. The interaction between `repAIrC` and the database is achieved by means of JDBC, a Java database connectivity technology able to interface with nearly all existing SQL databases. In order to determine whether an AIC is satisfied by a database, method `getUpdateActions` first builds a single SQL query corresponding to the body of the AIC. This method builds two separate `SELECT` statements, one for the positive and another for the negative literals in the body of the AIC. Each time a new variable is found, the table and column where it occurs are stored, so that future references to the same variable in a positive literal can be unified by using inner joins. The `select` statement for the negative literals is then connected to the other one using a `WHERE NOT EXISTS` condition. Variables in the negative literals must necessarily appear first in a positive literal in the same AIC; therefore, they can then be connected by a `WHERE` clause instead of an inner join.

Example 2. *The bodies of the integrity constraints in Example 1 generate the following SQL queries.*

```
SELECT * FROM junior
  INNER JOIN dept_emp
  ON junior.id=category.empId
  WHERE category.type='boss'

SELECT * FROM junior
  WHERE NOT EXISTS
 (SELECT * FROM insured
    WHERE insured.empId=junior.id
    AND insured.type='basic')
```

3.3 Implementing Repair Trees

The implementation of the repair trees directly follows the algorithms described in Section 2. Different types of repair trees are implemented using inheritance, so that most of the code can be reused in the more complex trees. The trees are constructed in a breadth-first manner, and all non-contradictory leaves that are found are stored in a list. At the end, this list is pruned so that only the minimal elements (w.r.t. set inclusion) remain – as these are the ones that correspond to repairs.

While constructing the tree, the database has to be temporarily updated and restored. Indeed, to calculate the descendants of a node, we first need to evaluate all AICs at that node in order to determine which ones are violated; this requires querying a modified version of the database that takes into account the update actions in the current node.

In order to avoid concurrency issues, these updates are performed in a transaction-style way, where we update the database, perform the necessary SQL queries, and rollback to the original state, guaranteeing that other threads interacting with the database during this process neither see the modifications nor lead to inconsistent repair trees. This becomes of particular interest when the parallel processing tools described in Section 4 are put into place. Although this adds some overhead to the execution time, at the end of that section we discuss why scalability is not a practically relevant concern.

After finding all the leaves of the repair tree, a further step is needed in the case one is looking for founded or justified repairs, as the corresponding trees may contain leaves that do not correspond to repairs with the desired property. This step is skipped if all AICs are normal, in view of the results from (Cruz-Filipe et al., 2013). For founded repairs, we directly apply the definition: for each action α, check that there is an AIC with α in its head and such that all other literals in its body are satisfied by the database.

For justified repairs, the validation step is less obvious. Directly following the definition requires constructing the set of no-effect actions, which is essentially as large as the database, and iterating over subsets of this set. This is obviously not possible to do in practical settings. Therefore, we use some criteria to simplify this step.

Lemma 1. *If a rule r was not applied in the branch leading to $\mathcal{U}$, then $\mathcal{U}$ is closed under r.*

Proof. Suppose that r was never applied and assume $\mathsf{nup}(r) \subseteq \mathsf{ne}(I, I \circ \mathcal{U})$. Then necessarily $\mathsf{head}(r) \cap \mathsf{ne}(I, I \circ \mathcal{U}) \neq \emptyset$, otherwise r would be applicable and $\mathcal{U}$ would not be a repair. $\square$

By construction, $\mathcal{U}$ is also closed for all rules applied in the branch leading to it.

Let $\mathcal{U}$ be a candidate justified weak repair. In order to test it, we need to show that $\mathcal{U} \cup \mathsf{ne}(I, I \circ \mathcal{U})$ is a justified action set (see (Cruz-Filipe et al., 2013)), which requires iterating over all subsets of $\mathcal{U} \cup$

$\mathrm{ne}(I, I \circ \mathcal{U})$ that contain $\mathrm{ne}(I, I \circ \mathcal{U})$. Clearly this can be achieved by iterating over subsets of $\mathcal{U}$.

But if $\mathcal{U}^* \subseteq \mathcal{U}$, then $\mathrm{nup}(r) \cap \mathcal{U}^* = \emptyset$; this allows us to simplify the closedness condition to: if $\mathrm{nup}(r) \subseteq \mathrm{ne}(I, I \circ \mathcal{U})$, then $\mathcal{U}^* \cap \mathrm{head}(r) = \emptyset$. The antecedent needs then only be done once (since it only depends on $\mathcal{U}$), whereas the consequent does not require consulting the database.

The following result summarizes these properties.

Lemma 2. *A weak repair $\mathcal{U}$ in a leaf of the justified repair tree for $\langle I, \eta \rangle$ is a justified weak repair for $\langle I, \eta \rangle$ iff, for every set $\mathcal{U}^* \subseteq \mathcal{U}$, if $\mathrm{nup}(r) \subseteq \mathrm{ne}(I, I \circ \mathcal{U})$, then $\mathcal{U}^* \cap \mathrm{head}(r) = \emptyset$.*

The different implementations of repair trees use different subclasses of the abstract class `Node`; in particular, nodes of `JustifiedRepairTrees` must keep track not only of the sets of update actions being constructed, but also of the sets of non-updatable actions that were assumed. These labels are stored as `Set<Action>` using `HashSet` from the Java library as implementation, as they are repeatedly tested for membership everytime a new node is generated.

For efficiency, repair trees maintain internally a set of the sets of update actions that label nodes constructed so far as a `Set<Node>`. This is used to avoid generating duplicate nodes with the same label. Since this set is used mainly for querying, it is again implemented as a `HashSet`. Nodes with inconsistent labels are also immediately eliminated, since they can only produce inconsistent leaves.

3.4 Interfacing with the User

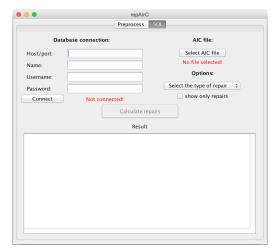The user interface for `repAIrC` is implemented using the standard Java GUI widget toolkit `Swing`, and is rather straightforward. On startup, the user is presented with the dialog box depicted in Figure 2.

The user can then provide credentials to connect to a database, as well as enter a file containing a set of AICs. If the connection to the database is successful and the file is successfully parsed, `repAIrC` invokes the `aicsCompatible` method required by the implementation of the `DB` interface (see Section 3.2) and verifies that all tables and columns mentioned in the set of AICs are valid tables and columns in the database. If this is not the case, then an error message is generated and the user is required to select new files; otherwise, the buttons for configuration and computation of repairs become active.

Once the initialization has succeeded, one can check the database for consistency and obtain different types of repairs, computed using the repair tree described above. As it may be of interest to obtain also weak repairs, the user is given the possibility of selecting whether to see only the repairs computed, or all valid leaves of the repair tree – which typically include some weak repairs. In both cases the necessary validations are performed, so that leaves that do not correspond to repairs (in the case of founded or justified repairs) are never presented.

An example output screen after successful computation of the repairs for an inconsistent database can be seen in Figure 3.

4 PARALLELIZATION AND STRATIFICATION

As described in Section 2.3, it is possible to parallelize the search for repairs of different kinds by split-

Figure 2: The initial screen for `repAIrC`.

Figure 3: Possible repairs of an inconsistent database.

ting the set of AICs into independent sets; in the case of founded or justified repairs, this parallelization can be taken one step further by also stratifying the set of AICs. Even though finding partitions and/or stratifications is asymptotically not very expensive (it can be solved in linear time by the well-known graph algorithms described below), it may still take noticeable time if the set of AICs grows very large.

Since, by definition, partitions and stratifications are independent of the actual database, it makes sense to avoid repeating their computation unless the set of AICs changes. For this reason, parallelization capabilities are implemented in `repAIrC` in a two-stage process. Inside `repAIrC`, the user can switch to the `Preprocess` tab, which provides options for computing partitions and stratifications of a set of AICs. This results in an annotated file which still can be read by the parser; in the main tab, parallel computation is automatically enabled whenever the input file is annotated in a proper manner.

4.1 Implementation

Computing optimal partitions in the spirit of (Cruz-Filipe, 2014) is not feasible in a setting where variables are present, as this would require considering all closed instances of all AICs – but it is also not desirable, as it would also result in a significant increase of the number of queries to the database. Instead, we work with the adapted definition of dependency given in Section 2. Given a set of AICs, `repAIrC` constructs the adjacency matrix for the undirected graph whose nodes are AICs and such that there is an edge between r_1 to r_2 iff r_1 and r_2 are not independent. A partition is then computed simply by finding the connected components in this graph by a standard graph algorithm.

The partitions computed are then written to a file, where each partition begins with the line

```
#PARTITION_BEGIN_[NO]#
```

where `[NO]` is the number of the current partition, and ends with

```
#PARTITION_END#
```

and the AICs in each partition are inserted in between, in the standard format.

To compute the partitions for stratification, we need to find the strongly connected components of a similar graph. This is now a directed graph where there is an edge from r_1 to r_2 if r_1 precedes r_2. The implementation is a variant of Tarjan's algorithm (Tarjan, 1972), adapted to give also the dependencies between the connected components.

The computed stratification is then written to a file with a similar syntax to the previous one, to which

a dependency section is added, between the special delimiters

```
#DEPENDENCIES_BEGIN#
```

and

```
#DEPENDENCIES_END#
```

The dependencies are included in this section as a sequence of strings `X -> Y`, one per line, where `X` and `Y` are the numbers of two partitions and `Y` precedes `X`.

Example 3. *The two AICs from Example 1 cannot be parallelized, as they both use the* `junior` *table, but they can be stratified, as only the first one makes changes to this table. Preprocessing this example by* `repAIrC` *would return the following output.*

```
#PARTITION_BEGIN_1#
junior(id = $X),
  category(type = boss, empId = $X)
  -> - junior(id = $X);
#PARTITION_END#
#PARTITION_BEGIN_2#
junior(id = $X),
  NOT insured(empId = $X, type = basic)
  -> + insured(empId = $X, type = basic);
#PARTITION_END#
#DEPENDENCIES_BEGIN#
2 -> 1
#DEPENDENCIES_END#
```

Imagine a simple scenario where the `junior` *table contains a single entry. Then, computing repairs for this set of AICs can be achieved by first repairing partition 1 (which will generate a tree with only one node) and then repairing the resulting database w.r.t. partition 2 (which builds another tree, also with only one node). By comparison, processing the two AICs simultaneously would potentially give a tree with 4 nodes, as both AICs would have to be considered at each stage.*

In general, if there are n entries in the `junior` table, the stratified approach will construct at most $n+1$ trees with a total of $n^2 + n$ nodes (one tree with n nodes for the first AIC, at most n trees with at most n nodes for the second AIC). By contrast, processing both AICs together will construct a tree with potentially $(2n)!$ leaves, which by removing duplicate nodes may still contain 2^{2n} nodes.

This example shows that, by stratifying AICs, we can actually get an exponential decrease on the size of the repair trees being built – and therefore also on the total runtime.

In addition to alleviating the exponential blowup of the repair trees, parallelization and stratification also allow for a multi-threaded implementation, where repair trees are built in parallel in multiple concurrent threads. To ensure that the dependencies be-

tween the partitions are respected, the threads are instructed to wait for other threads that compute preceding partitions. In Example 3, the thread processing partition 2 would be instructed to first wait for the thread processing partition 1 to finish.

Our empirical evaluation of `repAIrC` showed that speedups of a factor of 4 to 7 were observable even when processing small parallelizable sets of only two or three AICs. For larger sets of AICs, parallelization and stratification are necessary to obtain feasible runtimes. In one application, which allowed for 15 partitions to be processed independently, the stratified version computed the founded repairs in approximately 1 second, whereas the sequential version did not terminate within a time limit of 15000 seconds. This corresponds to a speedup of at least four orders of magnitude, demonstrating the practical impact of the contributions of this section.

4.2 Practical Assessment

In the worst case, parallelization and stratification will have no impact on the construction of the repair tree, as it is possible to construct a set of AICs with no independent subsets. However, the worst case is not the general case, and it is reasonable to believe that real-life sets of AICs will actually have a high parallelization potential.

Indeed, integrity constraints typically reflect high-level consistency requirements of the database, which in turn capture the hierarchical nature of relational databases, where more complex relations are built from simpler ones. Thus, when specifying *active* integrity constraints there will naturally be a preference to correct inconsistencies by updating the more complex tables rather than the most primitive ones.

Furthermore, in a real setting we are not so much interested in repairing a database once, but rather in ensuring that it remains consistent as its information changes. Therefore, it is likely that inconsistencies that arise will be localized to a particular table. The ability to process independent sets of AICs separately guarantees that we will not be repeatedly evaluating those constraints that were not broken by recent changes, focusing only on the constraints that can actually become unsatisfied as we attempt to fix the inconsistency.

For the same reason, scalability of the techniques we implemented is not a relevant issue: there is no practical need to develop a tool that is able to fix hundreds of inconsistencies efficiently simultaneously, since each change to the database will likely only impact a few AICs.

5 CONCLUSIONS AND FUTURE WORK

We presented a working prototype of a tool, called `repAIrC`, to check integrity of real-world SQL databases with respect to a given set of active integrity constraints, and to compute different types of repairs automatically in case inconsistency is detected, following the ideas and algorithms in (Flesca et al., 2004; Caroprese et al., 2007; Caroprese and Truszczyński, 2011; Cruz-Filipe et al., 2013; Cruz-Filipe, 2014). This tool is the first implementation of a concept we believe to have the potential to be integrated in current database management systems.

Our tool currently does not automatically apply repairs to the database, rather presenting them to the user. As discussed in (Eiter and Gottlob, 1992), such a functionality is not likely to be obtainable, as human intervention in the process of database repair is generally accepted to be necessary. That said, automating the generation of a small and relevant set of repairs is a first important step in ensuring a consistent data basis in Knowledge Management.

In order to deal with real-world heterogenous knowledge management systems, we are currently working on extending and generalizing the notion of (active) integrity constraints to encompass more complex knowledge repositories such as ontologies, expert reasoning systems, and distributed knowledge bases. The design of `repAIrC` has been with this extension in mind, and we believe that its modularity will allow us to generalize it to work with such knowledge management systems once the right theoretical framework is developed.

On the technical side, we are planning to speed up the system by integrating a local database cache for peforming the many update and undo actions during exploration of the repair trees without the overhead of an external database connection.

ACKNOWLEDGMENTS

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