

## DM553 – Complexity and Computability – 2016 Lecture 10

### Lecture, March 14

We finished chapter 5, skipping the last part of section 5.1, having to do with reductions via computation histories.

### Lecture, March 17 in U140

We will start with a course evaluation of how the course has been so far. Then, we will begin on NP-Completeness, introducing definitions and showing that 3-SAT is NP-Complete. To do this, we assume that CNF-SAT is NP-Complete. The proof that 3-SAT is NP-Complete combines the proofs in both the Sipser and the CLRS books. The definition of time complexity classes is on page 279 in Sipser's textbook, and the definition of P is on page 286. The definitions of NP and NP-Complete are in sections 7.3 and 7.4 of Sipser's textbook. Note that some of this is also in chapter 34 in the CLRS book.

### Lecture, March 29

We will cover the proof that SATISFIABILITY (actually CNF-SAT) is NP-Complete, from section 7.4 in Sipser's textbook. If there is time, we will do more reductions from chapter 34 in CLRS.

### Problems to be discussed in U155 on April 1

In the CLRS textbook, do the following:

1. 34.1-3, 34.1-5, 34.2-3.
2. Suppose that there is a language  $L$  for which there is an algorithm that accepts any string  $x \in L$  in polynomial time and rejects any  $x \notin L$ , but this algorithm runs in super-polynomial (more than polynomial) time if  $x \notin L$ . Argue that  $L$  can be decided in polynomial time.
3. 34.2-4 (skip Kleene star), 34.2-8.
4. 34.3-7 (34.3-6 has the definition of complete you need).