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- computing with floating point numbers
- compressing data
- executing machine code

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Program: representation of an algorithm

Pseudocode: representation of an algorithm

Process: execution of an algorithm

Art of problem solving

Polya's principles applied to algorithms:

1. Understand the problem
2. Get an idea for a possible algorithmic procedure (to solve it)
3. Formulate the algorithm and represent it as a program
4. Evaluate the program for correctness and its potential as a tool for solving other problems

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Not so easy as $1 \rightarrow 2 \rightarrow 3 \rightarrow 4$.

Examples:

- Magic trick — ideas, discover they don't work with some initial cards...
- 3 politicians (no names) A, B, C — know each other
 - ◆ 1 always tells the truth
 - ◆ 1 always lies
 - ◆ 1 does some of each
 - ◆ Ask 3 true/false questions
 - choose whichever politician you like for whichever question
 - determine which politician is which

Techniques:

- Brute force
- Stepwise refinement (top-down)
 - ◆ break into smaller and smaller problems
 - ◆ if modular (relatively independent) parts, can program in teams — software engineering

Cute problems in textbook.

Example: Step from pier into a boat

Hat falls into water.

River flows 2.5 miles/hour

Go upstream at 4.75 miles/hour

After 10 minutes discover hat missing.

Turn around to travel downstream.

How long before you get to the hat?

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Answer: 10 minutes

— It pays to think.

Pseudocode

- easier to read than a program
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- easier to read than a program
- syntax less important
- constructs from many languages work the same
 - ◆ `if...then...else` — condition is Boolean
 - ◆ `while`
 - ◆ `repeat`
 - ◆ `for`
 - ◆ `recursion`

Pseudocode

Types — use consistently and clearly

Incorrect example: $r \leftarrow \text{List} - c$

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Types — use consistently and clearly

Incorrect example: $r \leftarrow \text{List} - c$

Incorrect example: using n to be index and n th element of List

Must explain the general idea and what variables are used for if not obvious — not what it does, but why, in `if...then...else` clause for example.

Sequential search

Algorithms

Sequential Search

Sequential search problem:

Input: List of elements, TargetValue

Output: **success** if TargetValue is in List
failure if it is not in List

A brute force algorithm.

Sequential search

Algorithms

Sequential Search

```
procedure Search(List, TargetValue):  
{ Input: List is a list; TargetValue is a possible entry }  
{ Output: success if TargetValue in List; failure otherwise }
```

```
    if (List empty)  
        then Output failure  
  
    else  
        TestEntry ← 1st entry in List  
        while (TargetValue ≠ TestEntry  
              and there are entries not considered)  
            do (TestEntry ← next entry in List)  
        if (TargetValue = TestEntry)  
            then Output success  
            else Output failure
```

Analysis:

- time
- fundamental operation
 - ◆ takes time
 - ◆ number of occurrences proportional to everything else that happens

Analysis:

| List | = n

How many **comparisons** are necessary in the worst case?

A. 1

B. $n - 1$

C. n

D. $n + 1$

E. $2n$

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Analysis:

| List | = n

How many comparisons are necessary in the worst case?

D. $n + 1$

This is $\Theta(n)$.

Analysis:

What does $\Theta(n)$ meant?

Need to define $O(n)$ too.

$g \in O(f)$ means $\exists c, d$ s.t. $g(n) \leq c \cdot f(n) + d$

$g \in \Theta(f)$ means $g \in O(f)$ and $f \in O(g)$.

Sequential search

Analysis:

$g \in O(f)$ means $\exists c, d$ s.t. $g(n) \leq c \cdot f(n) + d$

$g \in \Theta(f)$ means $g \in O(f)$ and $f \in O(g)$.

Examples:

- $2n + 3 \in \Theta(n)$
- $3 \log n \in \Theta(\log n)$
- $2n + 7 \log n \in \Theta(n)$
- $4 \log n + m \in \Theta(\log n)$ if $m \leq \log n$
- Can write $\Theta(\log n + m)$ if unsure which term is larger.

Analysis:

What is $n \log n - 1.4n + 15$?

- A. $O(n^2)$
- B. $O(n \log n)$
- C. $\Theta(n \log n)$
- D. all of the above
- E. none of the above

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Sequential search — correctness

```
procedure Search(List, TargetValue):
  if (List empty)
    then Output failure
  else
    TestEntry ← 1st entry in List
    { precondition: TestEntry is 1st entry in List }
    while (TargetValue ≠ TestEntry
           and there are entries not considered)
      do (TestEntry ← next entry in List)
    { loop invariant: TargetValue ≠ any entry before TestEntry }
    { postcondition: either TargetValue = TestEntry
    or all entries considered and TargetValue not in List }
    if (TargetValue = TestEntry)
      then Output success
      else Output failure
```

Assertions

- statements which can be proven to hold (induction)
- at different points in program
- examples: precondition, postcondition, loop invariant

Proof by induction on number of times through the loop:

Proof verification: automated?

Sequential search — correctness

Algorithms

Sequential Search