

On-Line Algorithms – F04 – Lecture 5

Lecture, February 25

Kim Skak Larsen lectured, covering chapter 3 in the textbook, and the algorithm RAND in chapter 4.

Lecture, March 3

Kim Skak Larsen will finish chapter, and I will begin on chapter 6.

Lecture, March 10

We will finish chapter 6.

Problems for Monday, March 8

1. Do Exercise 4.2 in the textbook.
2. Do Exercise 4.3 in the textbook.
3. Do Exercise 4.5 in the textbook.
4. Do Exercise 4.6 in the textbook.
5. Consider an optimal offline paging algorithm. Find arbitrarily long request sequences with more than k pages for which it does not help OPT if it had more than k pages in its fast memory (i.e. OPT should have the same number of page faults with k pages as it would have with more pages).
6. Consider an algorithm with lookahead s , meaning that when deciding what to do about the current page request, the algorithm can see the next s requests before deciding what to do.

- Prove that any such deterministic algorithm has competitive ratio at least k .
- Consider $\text{LRU}(s)$, the algorithm which uses the LRU rule, ignoring (and never evicting) any page in the next s requests. Show that it does at least as well as LRU on any request sequence (assuming they start with the same pages in fast memory).