## the paths to choreography extraction

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## outline

## background

## choreography

extraction
choreographic programming
context choreographies

- high-level descriptions of communicating systems
- directed communication (from alice to bob)
- automatic compilation to process calculi
- good theoretical properties


## choreographic programming

context choreographies

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- automatic compilation to process calculi
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previously core choreographies
- minimal primitives for turing completeness
- captures the "essence" of choreographies


## choreographic programming

context choreographies

- high-level descriptions of communicating systems
- directed communication (from alice to bob)
- automatic compilation to process calculi
- good theoretical properties
previously core choreographies
- minimal primitives for turing completeness
- captures the "essence" of choreographies
in this work inverting compilation
- extraction from implementations
syntax

$$
\begin{aligned}
& C::= \mathbf{0}|\eta ; C| \text { if }(\mathrm{p} \cdot *=\mathrm{q} \cdot *) \text { then } C_{1} \text { else } C_{2} \\
& \mid \operatorname{def} X=C_{2} \text { in } C_{1} \mid X \\
& \eta::=\mathrm{p} \cdot e \rightarrow \mathrm{q} \mid \mathrm{p} \rightarrow \mathrm{q}[/] \\
& I::=\text { labels (at least two distinct) } \\
& e::=\text { some set of expressions }
\end{aligned}
$$

core choreographies (ii/ii)

$$
\begin{gathered}
\frac{v=e[\sigma(\mathrm{p}) / *]}{\mathrm{p} . e \rightarrow \mathrm{q} ; C, \sigma \longrightarrow C, \sigma[\mathrm{q} \mapsto \mathrm{v}]} \\
\overline{\mathrm{p} \rightarrow \mathrm{q}[/] ; C, \sigma \longrightarrow C, \sigma} \\
\frac{i=1 \text { if } \sigma(\mathrm{p})=\sigma(\mathrm{q}), i=2 \text { else }}{\text { if }(\mathrm{p} . *=\mathrm{q} . *) \text { then } C_{1} \text { else } C_{2}, \sigma \longrightarrow C_{i}, \sigma} \\
C_{1}, \sigma \longrightarrow C_{1}^{\prime}, \sigma^{\prime} \\
\operatorname{def} X=C_{2} \text { in } C_{1}, \sigma \longrightarrow \operatorname{def} X=C_{2} \text { in } C_{1}^{\prime}, \sigma^{\prime} \\
C_{1} \preceq C_{1}^{\prime} \quad C_{1}^{\prime}, \sigma \longrightarrow C_{2}^{\prime}, \sigma^{\prime} \quad C_{2}^{\prime} \preceq C_{2} \\
C_{1}, \sigma \longrightarrow C_{2}, \sigma^{\prime}
\end{gathered}
$$

(last rule says that
e.g. p.e $\rightarrow \mathrm{q} ;$ r. $e^{\prime} \rightarrow \mathrm{s}, \sigma \longrightarrow$ p.e $\left.\rightarrow \mathrm{q}, \sigma^{\prime}\right)$

## stateful processes

target language

- send to/receive from a process
- offer a choice to/select an option from a process
- conditional
- recursive definition
epp the endpoint projection of a choreography is a process term that implements the corresponding choreography
example the choreography

$$
\text { p.e } \rightarrow \text { q; p. } e^{\prime} \rightarrow r
$$

projects to

$$
\mathrm{p} \triangleright \mathrm{q}!e ; \mathrm{r}!e^{\prime}|\mathrm{q} \triangleright \mathrm{p} ?| \mathrm{r} \triangleright \mathrm{p} ?
$$

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## the problem

## questions

given a process network $N$ :

- is there a choreography $C$ with the same behaviour (bisimilarity)?
- in the affirmative case, can we construct $C$ from $N$ ?


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answer no
- undecidability results prevent perfect solution
... but can we solve this for a large enough set of $N$ ?


## the problem

questions
given a process network $N$ :

- is there a choreography $C$ with the same behaviour (bisimilarity)?
- in the affirmative case, can we construct $C$ from $N$ ?
answer no
- undecidability results prevent perfect solution
- ... but can we solve this for a large enough set of $N$ ?
new goal given a process network $N$ :
- if we return yes, we can build $C$ bisimilar to $N$
- we return yes as much as possible


## our approach

idea symbolic execution of $N$ (abstracting from values, two cases in conditionals) each "path" corresponds to a choreography

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$$
\begin{aligned}
& \mathrm{p} \triangleright \mathrm{q}!e ; \mathrm{r}!e^{\prime}|\mathrm{q} \triangleright \mathrm{p} ?| \mathrm{r} \triangleright \text { if } *=\mathrm{p} . * \text { then } \mathbf{0} \text { else } \mathrm{q} \text { ? } \\
& \downarrow^{p . e \rightarrow q}
\end{aligned}
$$

## our approach

idea symbolic execution of $N$ (abstracting from values, two cases in conditionals) each "path" corresponds to a choreography

extracted choreography p.e $\rightarrow \mathrm{q}$; if $\mathrm{r} . *=\mathrm{p} . *$ then $\mathbf{0}$ else $\mathbf{1}$
where $\mathbf{1}$ stands for deadlock (equivalent to $\mathbf{0}$ )

## properties (finite case)

- always terminates
- identifies potential problems by 1
- bisimilarity always holds!
- non-deterministic (up to structural equivalence)
- is sound and (almost) complete (deadlocks may occur in dead code)


## introducing recursion

the problem
consider the following networks

$$
\begin{aligned}
\mathrm{p} \triangleright \operatorname{def} X & =\mathrm{q}!* ; X \text { in } X \\
\mid \mathrm{q} \triangleright \operatorname{def} Y & =\mathrm{p} ? ; Y \text { in } Y
\end{aligned}
$$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X
$$

$$
\mid q \triangleright \operatorname{def} Y=p ? ; Y \text { in } Y
$$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X
$$

$$
\mid q \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y
$$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X
$$

$$
\mid q \triangleright \operatorname{def} Y=p ? ; p ? ; Y \text { in } Y
$$

## introducing recursion

the problem consider the following networks

- $\quad \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X$ in $X$ $\mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p}$ ?; $Y$ in $Y$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X
$$

$$
\mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y
$$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X
$$

$$
\mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y
$$

$$
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X
$$

$$
\mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; \mathrm{p} ? ; Y \text { in } Y
$$

main intuition
we do not care what the recursive definitions at the processes say!
the idea do the same as before, but allow loops

## introducing recursion

the problem
consider the following networks

$$
\begin{aligned}
& \begin{aligned}
\mathrm{p} \triangleright \operatorname{def} X & =\mathrm{q}!* ; X \text { in } X \\
\mathrm{q} \triangleright \operatorname{def} Y & =\mathrm{p} ? ; Y \text { in } Y \quad \rightsquigarrow \operatorname{def} X=\mathrm{p} . e \rightarrow \mathrm{q} ; X \text { in } X \\
\mathrm{p} \triangleright \operatorname{def} X & =\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
\mid \mathrm{q} \triangleright \operatorname{def} Y & =\mathrm{p} ? ; Y \text { in } Y \\
\mathrm{p} \triangleright \operatorname{def} X & =\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X \\
\mid \mathrm{q} \triangleright \operatorname{def} Y & =\mathrm{p} ? ; Y \text { in } Y \\
\mathrm{p} \triangleright \operatorname{def} X & =\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
\mid \mathrm{q} \triangleright \operatorname{def} Y & =\mathrm{p} ? ; \mathrm{p} ? ; Y \text { in } Y \\
& \mathrm{p} \triangleright X \mid \mathrm{q} \triangleright Y
\end{aligned}
\end{aligned}
$$

## introducing recursion

the problem
■

■

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\mathrm{p} . e \rightarrow \mathrm{q} ; X \text { in } \mathrm{p} . e \rightarrow \mathrm{q} ; X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; \mathrm{p} ? ; Y \text { in } Y
\end{aligned}
$$

$$
\mathrm{p} \triangleright \mathrm{q}!* ; X|\mathrm{q} \triangleright Y \xrightarrow{\mathrm{p} . e \rightarrow \mathrm{q}} \mathrm{p} \triangleright X| \mathrm{q} \triangleright Y \quad \mathrm{p} \cdot e \rightarrow \mathrm{q}
$$

## introducing recursion

the problem
■
-

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\mathrm{p} . e \rightarrow \mathrm{q} ; X \text { in } \mathrm{p} . e \rightarrow \mathrm{q} ; X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\mathrm{p} . e \rightarrow \mathrm{q} ; \mathrm{p} . e \rightarrow \mathrm{q} ; X \text { in } X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; \mathrm{p} ? ; Y \text { in } Y
\end{aligned}
$$

$$
\mathrm{p} \triangleright X \mid \mathrm{q} \triangleright \underset{\mathrm{p} . e \rightarrow \mathrm{q}}{\stackrel{\mathrm{p} . e \rightarrow \mathrm{q}}{\underset{Y_{\mathrm{p}}}{\gtrless}} \mathrm{q}!* ; X \mid \mathrm{q} \triangleright Y}
$$

## introducing recursion

$$
\mathrm{p} \triangleright \mathrm{q}!* ; X \mid \mathrm{q} \triangleright \underset{\underset{\mathrm{p} . e \rightarrow \mathrm{q}}{\stackrel{\mathrm{p} . e \rightarrow \mathrm{q}}{Y}} \underset{\mathrm{p}}{\stackrel{\mathrm{p}}{\underset{~}{~}}} X \mid \mathrm{q} \triangleright \mathrm{p} ? ; Y}{ }
$$

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \quad \rightsquigarrow \operatorname{def} X=\mathrm{p} . e \rightarrow \mathrm{q} ; X \text { in } X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} \text { ?; } Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\text { p.e } \rightarrow \mathrm{q} ; X \text { in p.e } \rightarrow \mathrm{q} ; X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } X \\
& \mid q \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\text { p.e } \rightarrow \mathrm{q} ; \text { p.e } \rightarrow \mathrm{q} ; X \text { in } X \\
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; \mathrm{q}!* ; X \text { in } \mathrm{q}!* ; X \\
& \mid q \triangleright \operatorname{def} Y=\mathrm{p} ? ; \mathrm{p} \text { ?; } Y \text { in } Y \\
& \rightsquigarrow \operatorname{def} X=\text { p.e } \rightarrow \mathrm{q} ; \text { p.e } \rightarrow \mathrm{q} ; X \text { in } X
\end{aligned}
$$

## fairness and starvation

problems not all loops are equal...

$$
\begin{array}{r}
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
\mid \mathrm{r} \triangleright \operatorname{def} Z=\mathrm{s}!* ; Z \text { in } Z \mid \mathrm{s} \triangleright \operatorname{def} W=\mathrm{r} ? ; W \text { in } W \\
\underbrace{\mathrm{p} \triangleright X \mid \mathrm{q} \triangleright Y}_{\mathrm{p} \cdot * \rightarrow \mathrm{q}}
\end{array}
$$

extracts to $\operatorname{def} X=\mathrm{p} . * \rightarrow \mathrm{q} ; X$ in $X$ or $\operatorname{def} X=\mathrm{r} . * \rightarrow \mathrm{~s} ; X$ in $X$

## fairness and starvation

problems not all loops are equal. . .

$$
\begin{array}{r}
\mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
\mid \mathrm{r} \triangleright \operatorname{def} Z=\mathrm{s}!* ; Z \text { in } Z \mid \mathrm{s} \triangleright \operatorname{def} W=\mathrm{r} ? ; W \text { in } W
\end{array}
$$

solution annotate procedure calls


## fairness and starvation

problems not all loops are equal...

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
&|\mathrm{r} \triangleright \mathrm{~s}!*| \mathrm{s} \triangleright \mathrm{r} ? \\
&> \mathrm{p} \triangleright X \mid \mathrm{q} \triangleright Y \\
& \mathrm{p} \cdot * \rightarrow \mathrm{q}
\end{aligned} \mathrm{r} \triangleright \mathrm{~s}!*|\mathrm{~s} \triangleright \mathrm{r} ? \xrightarrow{\mathrm{r} \cdot * \rightarrow \mathrm{~s}} \mathrm{p} \triangleright X| \underbrace{\mathrm{q} \triangleright Y}_{\mathrm{p} \cdot * \rightarrow \mathrm{q}}
$$

extracts to $\operatorname{def} X=\mathrm{p} . * \rightarrow \mathrm{q} ; X$ in $X$ or $\operatorname{def} X=\mathrm{p} . * \rightarrow \mathrm{q} ; X$ in $\mathrm{r} . * \rightarrow \mathrm{~s} ; X$

## fairness and starvation

not all loops are equal. . .

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
&|\mathrm{r} \triangleright \mathrm{~s}!*| \mathrm{s} \triangleright \mathrm{r} ? \\
&> \mathrm{p} \triangleright X \mid \mathrm{q} \triangleright Y \\
& \mathrm{p} \cdot * \rightarrow \mathrm{q}
\end{aligned} \mathrm{r} \triangleright \mathrm{~s}!*|\mathrm{~s} \triangleright \mathrm{r} ? \xrightarrow{\mathrm{r} \cdot * \rightarrow \mathrm{~s}} \mathrm{p} \triangleright X| \underbrace{\mathrm{q} \triangleright Y}_{\mathrm{p} \cdot * \rightarrow \mathrm{q}}
$$

extracts to $\operatorname{def} X=\mathrm{p} . * \rightarrow \mathrm{q} ; X$ in $X$ or def $X=\mathrm{p} . * \rightarrow \mathrm{q} ; X$ in $\mathrm{r} . * \rightarrow \mathrm{~s} ; X$
solution no finite behaviour in loops (except deadlocks)

## fairness and starvation

problems not all loops are equal. . .

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \mid \mathrm{r} \triangleright \operatorname{def} Z=\mathrm{q}!* ; Z \text { in } Z \\
& \mathrm{p} \triangleright X^{\circ}\left|\mathrm{q} \triangleright Y^{\circ}\right| \mathrm{r} \triangleright Z^{\circ} \xrightarrow{\mathrm{p} \cdot * \rightarrow \mathrm{q}} \mathrm{p} \triangleright X^{\bullet}\left|\mathrm{q} \triangleright Y^{\bullet}\right| \mathrm{r} \triangleright Z^{\circ}
\end{aligned}
$$

oops not extractable (but $r$ is deadlocked)

## fairness and starvation

problems not all loops are equal...

$$
\begin{aligned}
& \mathrm{p} \triangleright \operatorname{def} X=\mathrm{q}!* ; X \text { in } X \mid \mathrm{q} \triangleright \operatorname{def} Y=\mathrm{p} ? ; Y \text { in } Y \\
& \mid \mathrm{r} \triangleright \operatorname{def} Z=\mathrm{q}!* ; Z \text { in } Z \\
& \mathrm{p} \triangleright X^{\circ}\left|\mathrm{q} \triangleright Y^{\circ}\right| \mathrm{r} \triangleright Z^{\circ} \xrightarrow{\mathrm{p} \cdot * \rightarrow \mathrm{q}} \mathrm{p} \triangleright X^{\bullet}\left|\mathrm{q} \triangleright Y^{\bullet}\right| \mathrm{r} \triangleright Z^{\circ}
\end{aligned}
$$

oops not extractable (but $r$ is deadlocked)
in general some networks are not extractable

## results

- if symbolic execution does not generate a node from which some process is always deadlocked, then $N$ is extractable
- if $C$ is extracted from $N$, then $C$ and $N$ are bisimilar ( $C$ may contain deadlocks)
- extraction terminates in time $O\left(n \times e^{2 n / e}\right)$
- works for synchronous semantics
- can be adapted to/extended in the asynchronous case


## conclusions $E^{\mathcal{J}}$ future directions

- showed how to extract choreographies from implementations
- significant improvement in complexity wrt previous work
- prototype implementation nearly ready
- extension to process spawning in progress

