

## DM538 – Ugeseddel 11

### Uge 48

#### Forelæsning tirsdag d. 26/11

**NB:** Forelæsningen bliver ikke nødvendigvis om tirsdagen — jeg prøver at få skemalæggeren til at flytte den til et tidspunkt, hvor ingen har overlap — I får besked.

Kleinberg and Tardos:

- Vi afslutter afsnit 13.2: Global minimum cut
- Afsnit 13.3: Coupon Collector's Problem
- Afsnit 13.4: MAX 3-SAT
- Hvis der bliver tid, begynder vi på afsnit 13.5: Median finding and Quicksort

#### Øvelser fredag d. 29/11

- Cormen: opgave 5.3-2, 5.3-3, 5.3-4, 5.3-7  
Hint til opgave 5.3-3: Se på  $n = 3$ . Sammenlign antallet af mulige swap-sekvenser med antallet af permutationer af 3 elementer.
- Denne opgave er en omskrivning af en opgave fra Kleinberg and Tardos:  
This exercise is about *contention resolution*. We have a system with 10 processes. Certain pairs of processes are in conflict, meaning that they need access to the same resource. Hence, such a pair cannot run at the same time. Assume that each proces is in conflict with exactly 2 other processes.  
Consider the following randomized algorithm for finding a largest possible set  $S$  of processes that can run simultaneously.  
Each process independently picks a random value; it chooses 1 with probability  $p$  and 0 with probability  $1 - p$ .  
If it chooses 1, and all conflicting processes choose 0, then the process enters the set  $S$ .  
  
What is the optimal value of  $p$ ?  
What is the expected size of  $S$  for this value of  $p$ ?  
Assuming the above strategy is used  $t$  times, give a lower bound on the probability that all processes enter the set  $S$  at least once, for  $t = 25$  and  $t = 50$ .
- Eksamen januar 2013 opgave 3