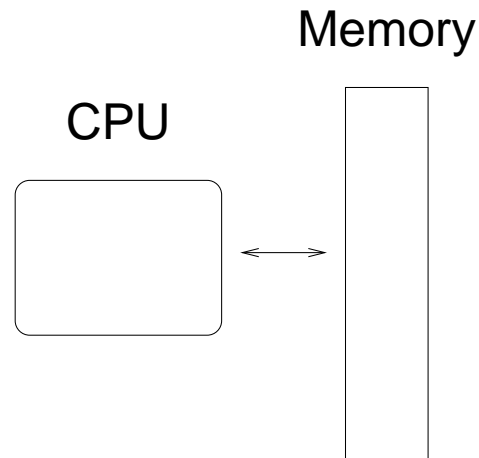


The I/O-Model

- Aggarwal and Vitter, *The Input/Output Complexity of Sorting and Related Problems*. Communications of the ACM, 31(9), p. 1116-1127, 1988.

Analysis of algorithms

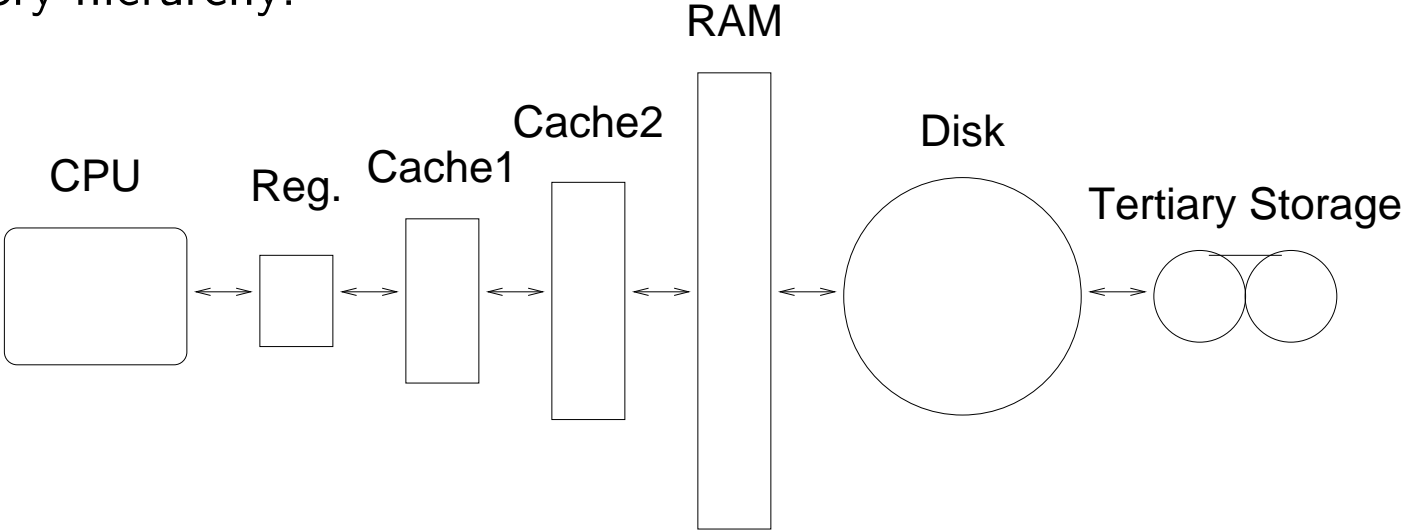
The standard model:



- **ADD**: 1 unit of time
- **MULT**: 1 unit of time
- **BRANCH**: 1 unit of time
- **MEMACCESS**: 1 unit of time

Reality

Memory hierarchy:



	<i>Access time</i>	<i>Volume</i>
Registers	1 cycle	1 Kb
Cache	5 cycles	512 Kb
RAM	50 cycles	256 Mb
Disk	2,000,000 cycles	80 Gb

CPU speed improves faster than RAM access time and **much** faster than disk access time

I/O bottleneck

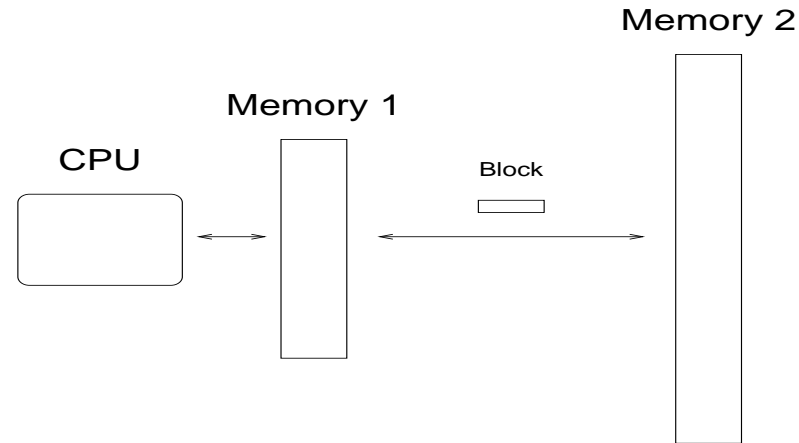
I/O is the bottleneck



I/O should be optimized (not instruction count)

Analysis of algorithms

New I/O-model:



Parameters:

N = no. of elements in problem.

M = no. of elements that fits in RAM.

B = no. of elements in a block on disk.

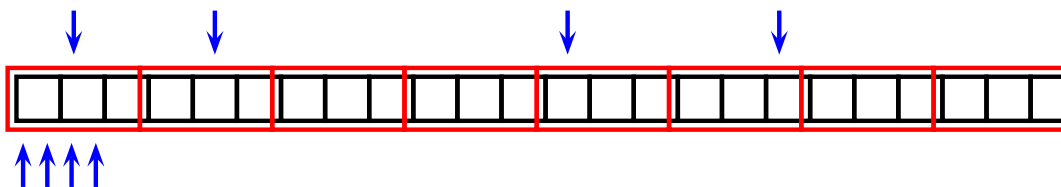
D = no. of disks (copies of Memory 2)

Cost: Number of I/O's (block transfers) between Memory 1 and Memory 2.

Generic Example

Consider two $O(n)$ algorithms:

1. Memory accessed randomly \Rightarrow page fault at each memory access.
2. Memory accessed sequentially \Rightarrow page fault every B memory accesses.



$O(N)$ I/Os vs. $O(N/B)$ I/Os

Typically, $B \sim 10^3$.

Specific Examples

Two classic sorting algorithms:

QuickSort \sim sequential access

vs.

HeapSort \sim random access

QuickSort: $O(N \log_2(N/M)/B)$ I/Os

HeapSort: $O(N \log_2(N/M))$ I/Os

Other examples:

- Hashing, radixsort (random access)
- Scanning, queues (sequential access)