Decomposing directed graphs into strongly connected spanning subdigraphs

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Conjecture1 (B-J, Yeo)

$\exists$ natural number N s.t
$\forall$ N-arc-strong digraph $D=(V,A)$
$\exists$ $A_1, A_2 \subseteq A$, $A_1 \cap A_2 = \emptyset$, $A_1 \cup A_2 = A$
s.t
$D_i = (V, A_i)$ is strong $i=1,2$

For tournaments $N=2$.

Conjecture2 (B-J, Yeo)

Every k-arc-strong tournament can be arc-decomposed into k spanning and strong subdigraphs.

True if
- $k=2$, or
- $\exists$ non-trivial cut of size k, or
- $\delta(T) \geq 37k$

Kelly Conjecture $\subseteq$ Conjecture 2