Three min/max theorems for coherent cyclic orders of digraphs. A proof of a conjecture of Gallai.

November 6, 2003

In a previous talk, Stéphan Thomassé introduced the notion of *coherent cyclic order* of a strong digraph. In collaboration with him, we proved three min/max theorems related to these cyclic orders. They concern cyclic equivalent of stability number, maximal feedback arc sets number and chromatic number of a digraph. We connect these numbers with particular configuration of circuits in the cyclic order.

In particular, the first theorem about cyclic independance number gives as corollary a proof of a conjecture of Gallai (1963): every strong digraph admits a spanning set of at most α circuits, where α is the independance number of the digraph.