Algorithms in Cheminformatics – DM840 (autumn 2021)

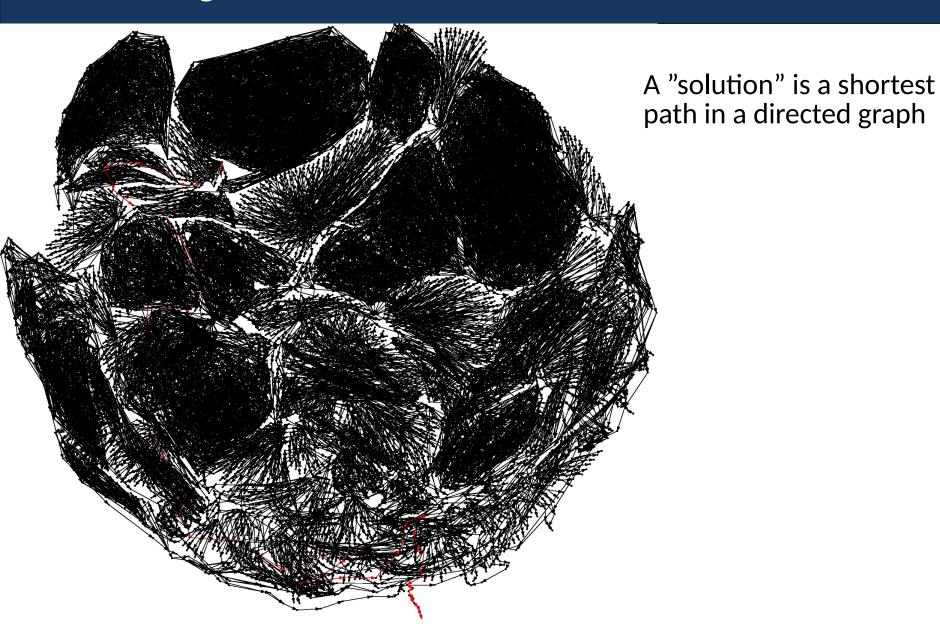
Daniel Merkle

LETS START WITH A GAME

(CATALAN)

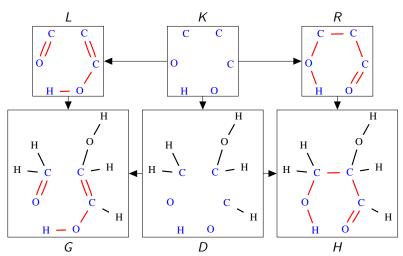
https://www.imada.sdu.dk/~daniel/DM840-2020/assignment1/assign1-2020.html https://www.imada.sdu.dk/~daniel/DM840-2021/ (For this slide set)

DM840 – Algorithms in Cheminformatics



Reactions – Application of Transformation Rules

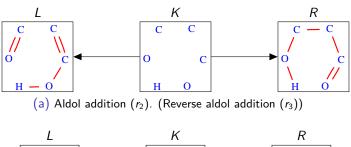
1,2-ethenediol + formaldehyde $\xrightarrow{\text{aldol addition}}$ glyceraldehyde

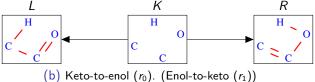


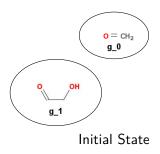
8

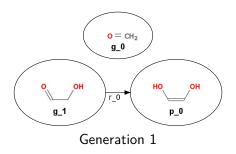
The Formose Chemistry

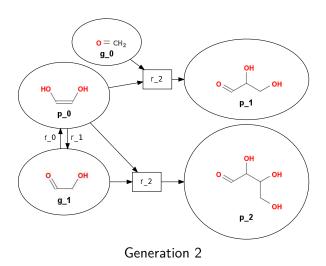
4 reaction patterns:

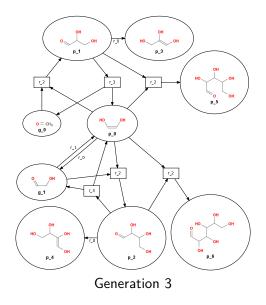


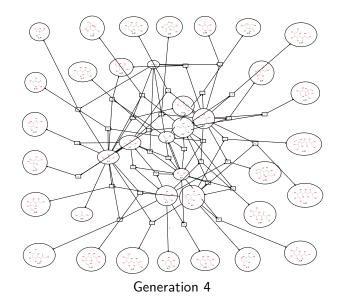




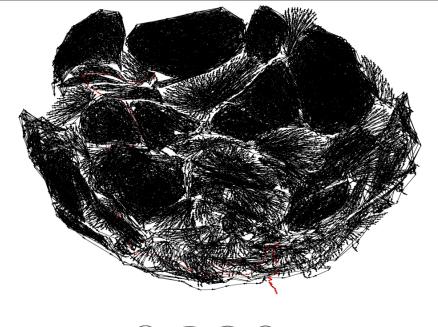




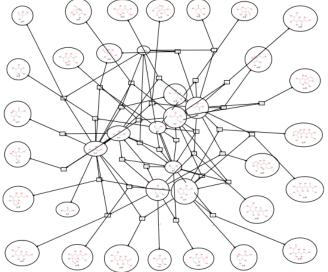




Shortest Path(s)

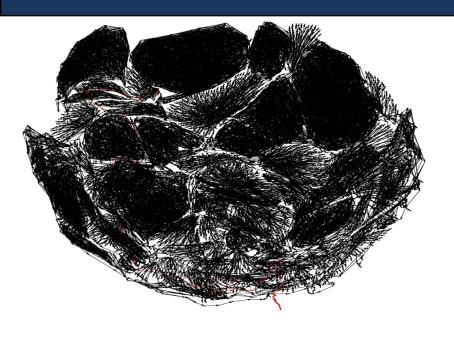


A "solution" is a shortest path in a directed graph

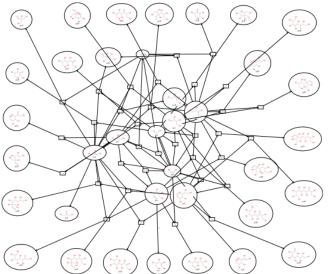


http://cheminf.imada.sdu.dk/mod

Shortest Path(s)



A "solution" is a shortest path in a directed graph



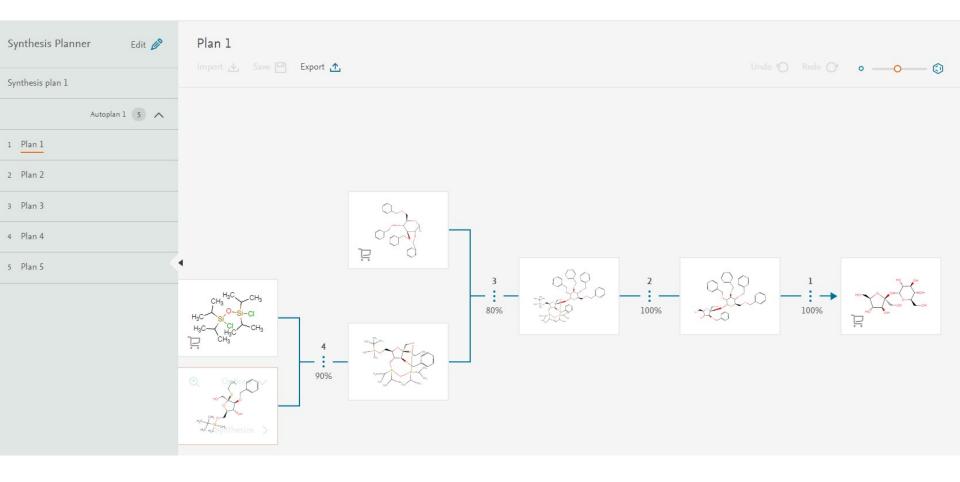
How to find the k best solutions?

In hypergraphs?

Algorithms?

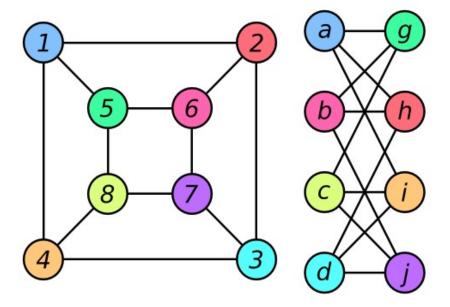
Computational Complexity?

How chemists do it



(Sub-)Graph Isomorphism / Canoncial Representations of Graphs

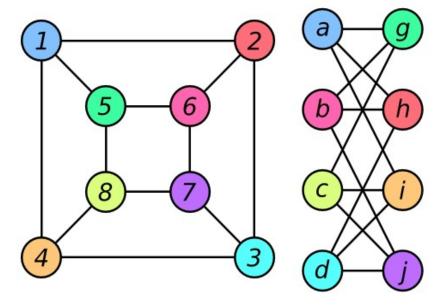
Are these 2 colored graphs isomorph?



Algorithms? Computational Complexity? State-of-the-Art?

(Sub-)Graph Isomorphism / Canoncial Representations of Graphs

Are these 2 colored graphs isomorph?



A Quasipolynomial Time Algorithm for Graph Isomorphism: The Details

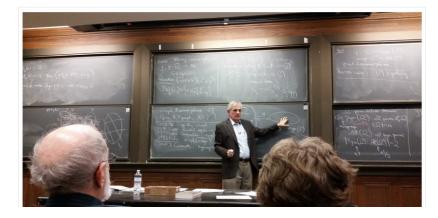
Posted on November 12, 2015 by j2kun

Update 2015-11-21: Ken Regan and Dick Lipton posted an article with some more details, and a high level overview of how the techniques fit into the larger picture of CS theory.

Update 2015-11-16: Laci has posted the talk on his website. It's an hour and a half long, and I encourage you to watch it if you have the time \circlearrowleft

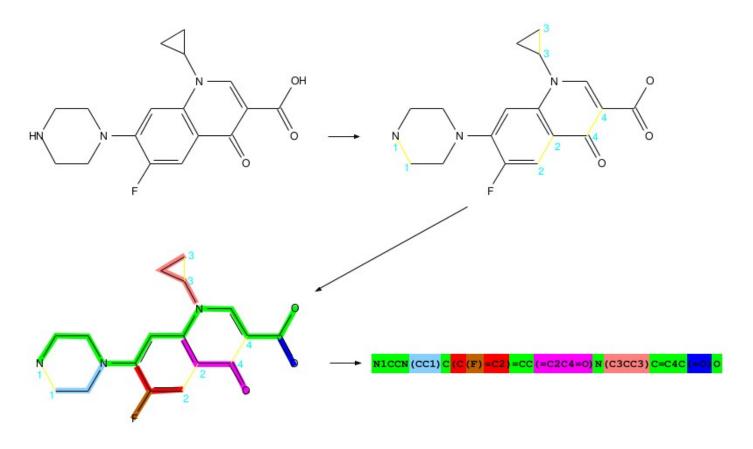
Laszlo Babai has claimed an astounding theorem, that the Graph Isomorphism problem can be solved in quasipolynomial time. On Tuesday I was at Babai's talk on this topic (he has yet to release a preprint), and I've compiled my notes here. As in Babai's talk, familiarity with basic group theory and graph theory is assumed, and if you're a casual (i.e., math-phobic) reader looking to understand what the fuss is all about, this is probably not the right post for you. This post is research level theoretical computer science. We're here for the juicy, glorious details.

Note: this blog post will receive periodic updates as my understanding of the details improve.



Algorithms? Computational Complexity? State-of-the-Art?

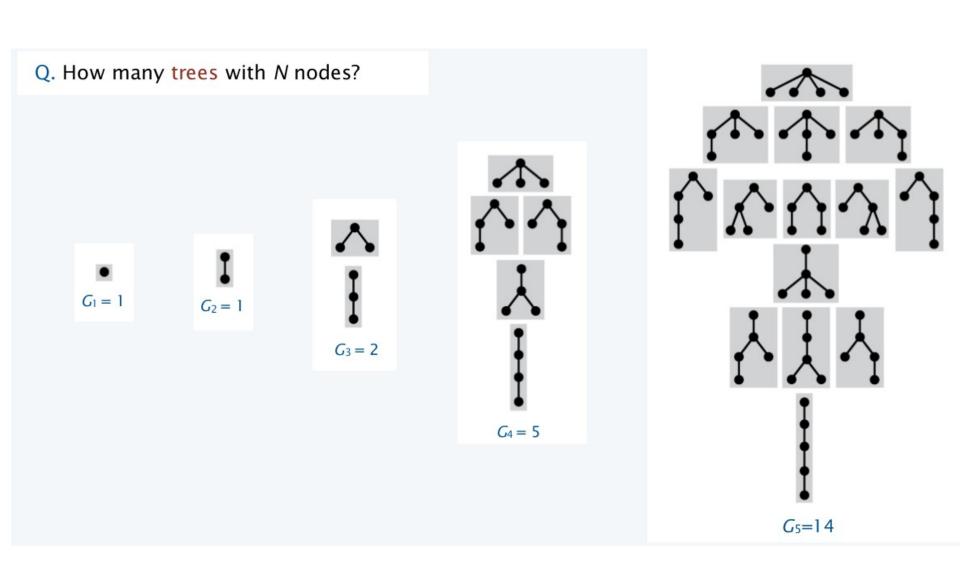
(Sub-)Graph Isomorphism / Canoncial Representations of Graphs



Canoncial representations of graphs (i.e. molecules):

Algorithms? Computational Complexity? And ... w.t.h. went wrong in Chemistry?

Counting



More Counting

Variations on a theme 1: Trees

Fundamental construct

Combinatorial class

G, the class of all trees

Construction

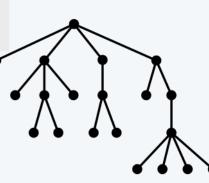
 $G = \bullet \times SEQ(G)$

"a tree is a node and a sequence of trees"

OGF equation

$$G(z) = z(1 + G(z) + G(z)^{2} + G(z)^{3} + ...) = \frac{z}{1 - G(z)}$$

$$G(z) - G(z)^2 = z$$



Variation on the theme: restrict each node to 0 or 2 children

Combinatorial class

T, the class of binary trees

Construction

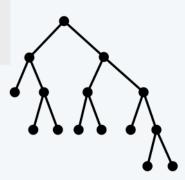
$$T = \bullet \times SEQ_{0,2}(T)$$

$$T = \bullet \times SEQ_{0,2}(T)^{\leftarrow}$$

OGF equation

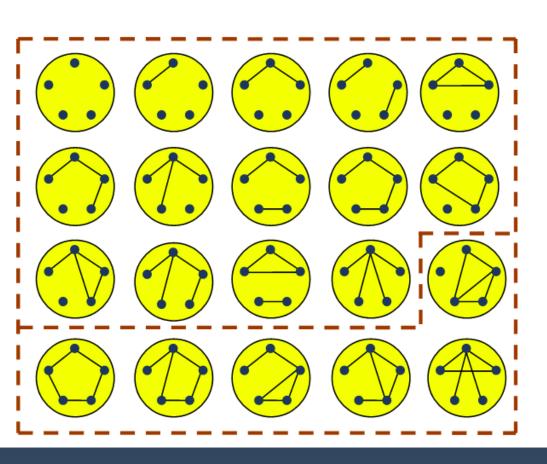
$$T(z) = z(1 + T(z)^2)$$

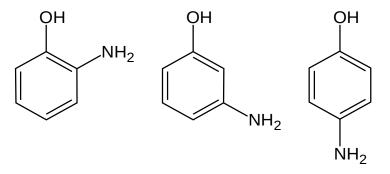
"a binary tree is a node and a sequence of 0 or 2 binary trees"



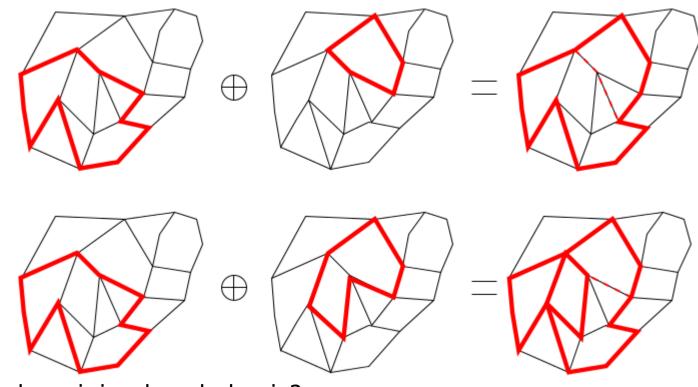
Applications: Sampling, Analysis of Algorithms, Chemistry

Even more counting



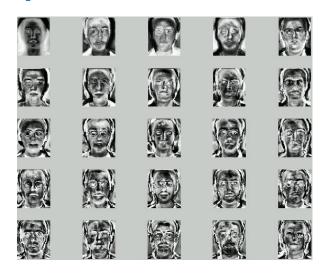


Cycle Bases (Scheduling, Distributed Computing, Chemistry)

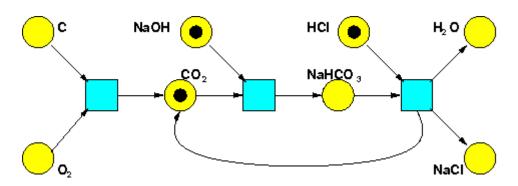


How to find a minimal cycle basis? Algorithms? Computaional Complexity? ...and w.t.h. went wrong in chemistry?

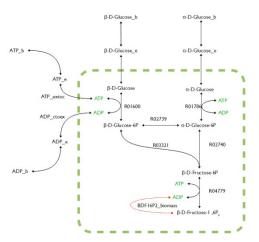
QSAR / PCA

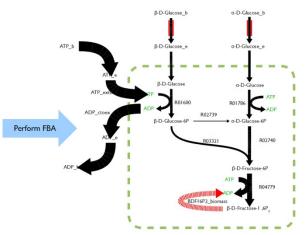


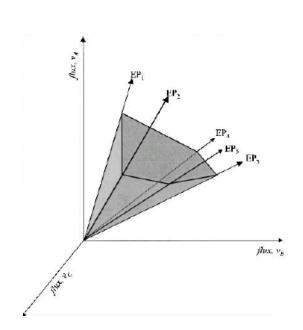
Petri Nets



Flux Balanced Analysis

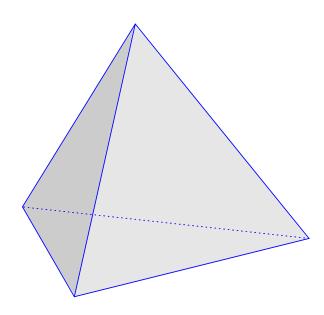




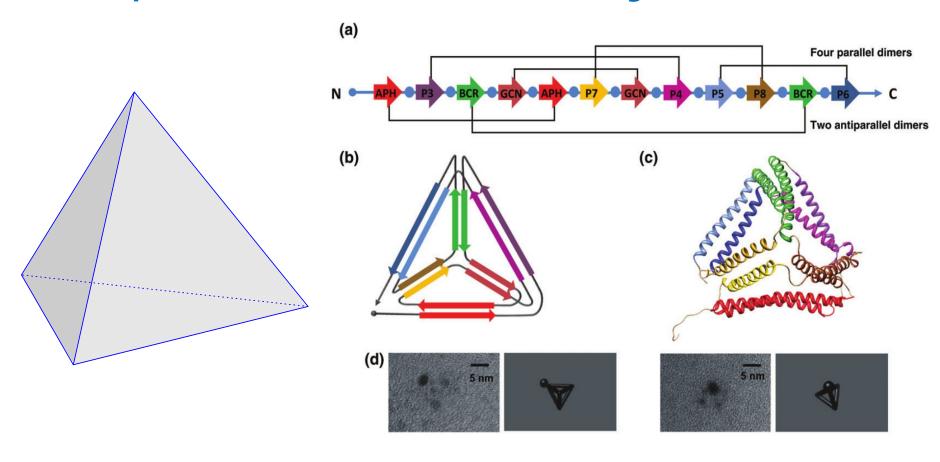


...and many more

For example: Traverse a tetrahedron, each edge twice.



...and many more For example: Traverse a tetrahedron, each edge twice.



Topics

Canonical Representations

Structure Descriptors

Graph Isomorphism

Pólya's Counting Theory

Artificial Chemistries

Graph Grammars

Cycle Bases

Metabolic Networks and Metabolic Pathways

Concurrency Theory

Petrinets

Applications in Industry

•••

Formal Model

Algorithms

Computational Complexity

Applications (including Chemistry)

Topics

Canonical Representations Structure Descriptors **Graph Isomorphism** Pólya's **Counting Theory**

Artificial Chemistries

Graph Grammars

Cycle Bases

Metabolic Networks and Metabolic Pathways

Concurrency Theory

Petrinets

Applications in Industry

•••

- 10 ECTS

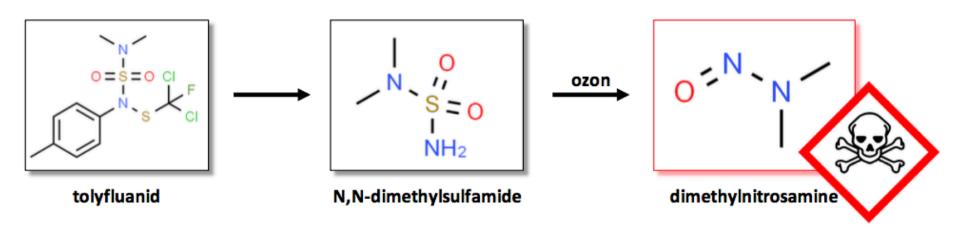
- max. 2 programming projects

no chemistry knowledge needed!





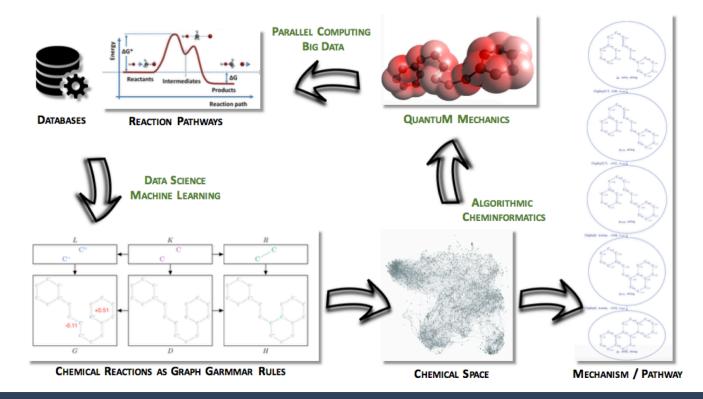












Enzyme Design

https://cheminf.imada.sdu.dk/novo-synergy/

